

# UNIT -02 COA DETAILED NOTES WITH EASY EXPLANATION AND DIAGRAMS

## Addition and Subtraction

★★★★★ Most Important Topic

Addition aur Subtraction Computer Arithmetic ka basic aur frequently asked topic hai.

Is topic se numericals bhi aate hain aur theory questions bhi.

Ye answer 3–4 pages aasani se cover karega.

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## Addition and Subtraction

### Introduction

Computer sirf binary numbers (0 aur 1) ko samajhta hai.

Isliye computer ke andar saare arithmetic operations binary form me perform kiye jate hain.

Addition aur Subtraction sabse basic arithmetic operations hain jinko ALU (Arithmetic Logic Unit) perform karta hai.

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### Definition

#### Binary Addition

**"Binary Addition is the process of adding two binary numbers according to binary arithmetic rules."**

## **Binary Subtraction**

**"Binary Subtraction is the process of subtracting one binary number from another using binary arithmetic rules."**

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# **Need of Addition and Subtraction**

Addition aur Subtraction ka use:

- Arithmetic calculations
- Data processing
- Scientific computations
- Computer programming
- Digital systems

me hota hai.

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# **Binary Number System Review**

Binary system me sirf do digits hoti hain:

0 and 1

Base = 2

---

# **Rules of Binary Addition**

Binary Addition ke basic rules:

| A | B | Sum | Carry |
|---|---|-----|-------|
| 0 | 0 | 0   | 0     |
| 0 | 1 | 1   | 0     |
| 1 | 0 | 1   | 0     |
| 1 | 1 | 0   | 1     |

## Important Rule

$$1 + 1 = 10$$

$$\text{Sum} = 0$$

$$\text{Carry} = 1$$

## Example 1: Binary Addition

Add:

```
1010
+
0101
```

Solution:

```
  1010
+ 0101
-----
  1111
```

Verification:

$$1010 = 10$$

$$0101 = 5$$

Result:

$$1111 = 15$$

Therefore:

$$10 + 5 = 15$$

Correct.

---

## Example 2: Binary Addition with Carry

Add:

$$\begin{array}{r} 1111 \\ + \\ 0001 \end{array}$$

Solution:

$$\begin{array}{r} 1111 \\ + 0001 \\ \hline 10000 \end{array}$$

Decimal Check:

$$15 + 1 = 16$$

Correct.

---

# Hardware for Binary Addition

Addition operation ke liye:

## Half Adder

## Full Adder

use kiye jate hain.

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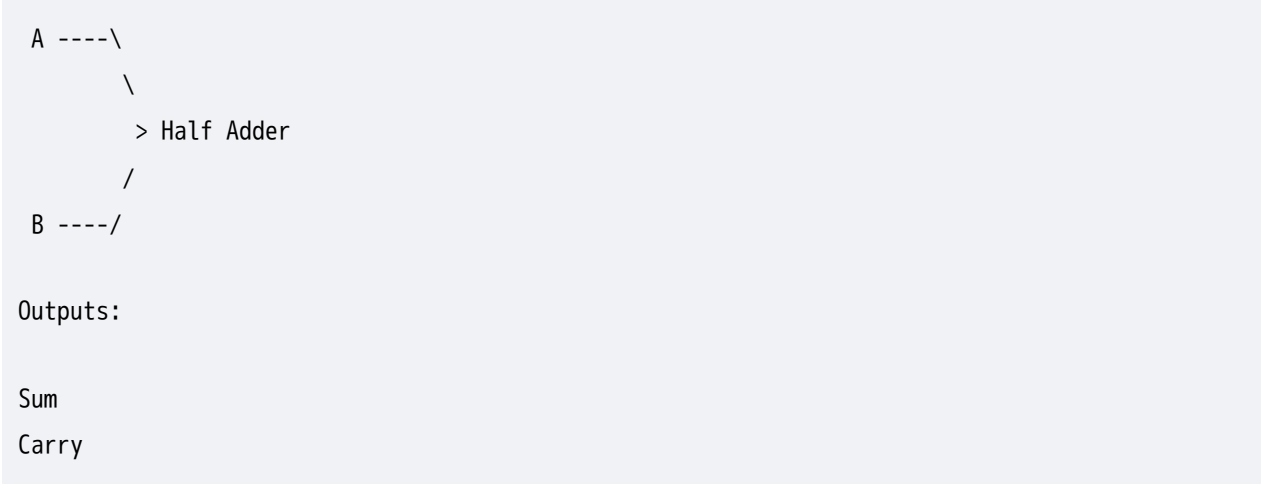
# Half Adder

## Definition

Half Adder ek combinational circuit hai jo do binary bits ko add karta hai.

---

## Block Diagram



## Truth Table

| A | B | Sum | Carry |
|---|---|-----|-------|
|---|---|-----|-------|

|   |   |   |   |
|---|---|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |

# Full Adder

## Definition

Full Adder teen inputs ko add karta hai.

A

B

Carry-In

## Block Diagram

```
A ----\  
      \  
B ----- > Full Adder  
      /  
Cin ----/  
  
Outputs:  
  
Sum  
Carry
```

## Truth Table

| A | B | Cin | Sum | Cout |
|---|---|-----|-----|------|
| 0 | 0 | 0   | 0   | 0    |
| 0 | 0 | 1   | 1   | 0    |
| 0 | 1 | 0   | 1   | 0    |
| 0 | 1 | 1   | 0   | 1    |
| 1 | 0 | 0   | 1   | 0    |
| 1 | 0 | 1   | 0   | 1    |
| 1 | 1 | 0   | 0   | 1    |
| 1 | 1 | 1   | 1   | 1    |

## Binary Subtraction

Binary subtraction bhi specific rules follow karti hai.

## Rules of Binary Subtraction

| A | B | Result              |
|---|---|---------------------|
| 0 | 0 | 0                   |
| 1 | 0 | 1                   |
| 1 | 1 | 0                   |
| 0 | 1 | 1 (Borrow Required) |

## Borrow Concept

0 - 1

Possible nahi hai.

Isliye left bit se borrow liya jata hai.

---

## Example 1: Binary Subtraction

Subtract:

```
1010
-
0011
```

Solution:

```
  1010
- 0011
-----
  0111
```

Verification:

```
10 - 3 = 7
```

Correct.

---

## Example 2: Subtraction Using Borrow

```
1000
-
0001
```

Solution:

```
 1000
- 0001
-----
 0111
```

Decimal:

```
8 - 1 = 7
```

Correct.

---

## Subtraction Using 2's Complement

Computer generally subtraction ko direct perform nahi karta.

Subtraction ko addition me convert kar deta hai.

Formula:

```
A - B
=
A + (2's Complement of B)
```

---

## Example

```
7 - 3
```

Binary:

```
7 = 0111
3 = 0011
```

2's Complement of 3:

0011

↓

1100 + 1

↓

1101

Now:

0111

+

1101

-----

10100

Discard Carry:

0100

Answer:

4

Correct.

---

## Addition and Subtraction Circuit

A

|

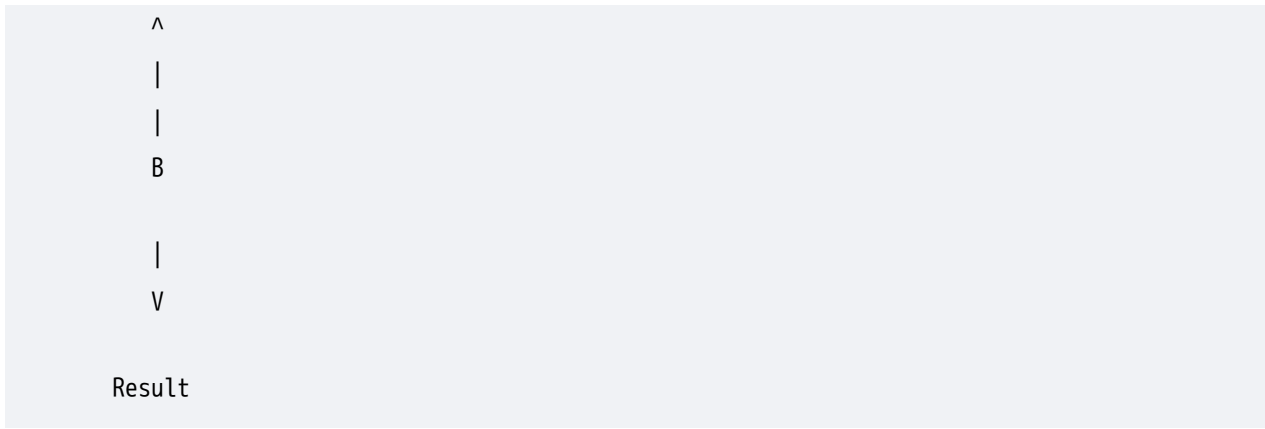
|

V

+-----+

| ALU |

+-----+



ALU addition aur subtraction dono perform karta hai.

---

## **Advantages of Binary Addition and Subtraction**

### **1. Simple Hardware**

Digital circuits me implementation easy hai.

---

### **2. High Speed**

Fast calculations possible.

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### **3. Reliable**

Error chances kam.

---

### **4. Suitable for Computers**

Binary system computer ke liye natural hai.

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## **Disadvantages**

## 1. Long Binary Numbers

Large numbers difficult lag sakte hain.

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## 2. Borrow and Carry Complexity

Manual calculations me complexity badh sakti hai.

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# Applications

## ALU Operations

CPU calculations.

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## Scientific Computing

Complex computations.

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## Embedded Systems

Microcontrollers.

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## Digital Signal Processing

DSP systems.

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# Difference Between Addition and Subtraction

| Addition              | Subtraction                |
|-----------------------|----------------------------|
| Numbers Add Hote Hain | Numbers Subtract Hote Hain |

|                         |                          |
|-------------------------|--------------------------|
| Carry Generate Hota Hai | Borrow Generate Hota Hai |
| Easier Operation        | Comparatively Complex    |
| Example: 5+3            | Example: 5-3             |

---

## Viva Questions

### Q1. What is Binary Addition?

Adding two binary numbers.

---

### Q2. What is Binary Subtraction?

Subtracting one binary number from another.

---

### Q3. What is Carry?

Extra bit generated during addition.

---

### Q4. What is Borrow?

Bit borrowed during subtraction.

---

### Q5. Which unit performs addition and subtraction?

ALU.

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## Frequently Asked RGPV Questions

### 2 Marks

1. Define Binary Addition.
  2. Define Binary Subtraction.
  3. What is Carry?
  4. What is Borrow?
- 

## 5 Marks

1. Explain Binary Addition.
  2. Explain Binary Subtraction.
  3. Explain Half Adder.
- 





## 7 Marks

1. Explain Binary Addition with examples.
  2. Explain Binary Subtraction with examples.
  3. Explain Full Adder.
- 

## 14 Marks

1. Explain Binary Addition and Subtraction with suitable examples.
  2. Discuss Half Adder and Full Adder with truth tables.
  3. Explain subtraction using 2's complement method.
- 

## Expected 2026 Questions

-  Explain Binary Addition and Binary Subtraction with examples.
-  Explain Half Adder and Full Adder.
-  Explain subtraction using 2's complement.
-  Perform binary addition and subtraction numerically.

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# One-Minute Revision

✓ Binary Addition:

$$1 + 1 = 10$$

✓ Binary Subtraction:

$$0 - 1 = \text{Borrow}$$

✓ Half Adder = 2 Inputs

✓ Full Adder = 3 Inputs

✓ ALU performs arithmetic operations

✓ Subtraction:

$$A - B$$

=

$$A + 2's \text{ Complement}(B)$$

---

## Conclusion

Addition and Subtraction computer arithmetic ke fundamental operations hain. Inhe binary number system ke rules ke according perform kiya jata hai. ALU in operations ko execute karta hai aur Half Adder, Full Adder aur 2's Complement techniques ki madad se fast aur efficient calculations perform ki jaati hain. Ye Computer Organization ka bahut important aur exam-oriented topic hai. 🎯

# 2's Complement Representation

★★★★★ Most Important Topic

2's Complement Representation Computer Arithmetic ka backbone hai.

RGPV me theory + numerical dono puchhe jate hain.

Ye answer 3–4 pages aasani se cover karega.

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## 2's Complement Representation

### Introduction

Computer positive aur negative numbers ko binary form me represent karta hai.

Negative numbers ko represent karne ke liye sabse common technique **2's Complement Representation** hai.

Computer arithmetic me subtraction aur signed arithmetic operations ko perform karne ke liye 2's Complement ka use kiya jata hai.

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### Definition

"2's Complement is a method of representing negative binary numbers in which 1 is added to the 1's complement of a binary number."

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## Why 2's Complement is Used?

### 1. Negative Numbers Representation

Negative numbers ko easily represent karta hai.

## 2. Simplifies Arithmetic

Subtraction ko addition me convert kar deta hai.

## 3. Single Hardware

Same adder circuit addition aur subtraction dono perform kar sakta hai.

## 4. Efficient Processing

Computer arithmetic fast ho jati hai.

---

# Binary Complements

Binary arithmetic me do types ke complements use hote hain:

## 1. 1's Complement

## 2. 2's Complement

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# 1's Complement

Binary number ke har bit ko invert kar diya jata hai.

## Rule

$0 \rightarrow 1$

$1 \rightarrow 0$

---

## Example

Binary Number:

1010

1's Complement:

0101

---

## 2's Complement

2's Complement nikalne ke liye:

### Step 1

1's Complement nikalo.

### Step 2

Usme 1 add karo.

---

## Formula

2's Complement

=

1's Complement + 1

---

## Example 1

Find 2's Complement of:

1010

---

## Step 1: 1's Complement

1010

↓

0101

---

## Step 2: Add 1

0101

+

0001

-----

0110

Answer:

0110

---

## Example 2

Find 2's Complement of:

1100

---

### Step 1

1100

↓

0011

---

### Step 2

```
0011
+
0001
-----
0100
```

Answer:

```
0100
```

---

## Shortcut Method

### Rule

Right side se first 1 tak bits same rakho.

Baaki sab bits invert kar do.

---

### Example

```
101100
```

Rightmost 1 tak same:

```
100
```

Remaining invert:

```
010
```

Answer:

```
010100
```

---

# Representation of Positive and Negative Numbers

## Positive Number

MSB = 0

Example:

+5

00000101

---

## Negative Number

MSB = 1

Example:

-5

First:

5 = 00000101

1's Complement:

11111010

2's Complement:

11111011

Therefore:

-5 = 11111011

---

## Range of Numbers in 8-bit 2's Complement

Formula:

$-(2^{(n-1)})$   
to  
 $(2^{(n-1)}-1)$

---

For 8-bit:

-128 to +127

---

## Representation Table

| Decimal | Binary (8-bit) |
|---------|----------------|
| +5      | 0000101        |
| -5      | 11111011       |
| +10     | 0001010        |
| -10     | 11110110       |

---

## Subtraction Using 2's Complement

Most Important

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**Formula**

$A - B$

$=$

$A + 2\text{'s Complement}(B)$

---

## Example

Find:

$7 - 3$

---

### Step 1

Convert to binary

$7 = 0111$

$3 = 0011$

---

### Step 2

Find 2's Complement of 3

0011

↓

1100

↓

1101

---

### Step 3

Add

```
0111
+
1101
-----
10100
```

Discard Carry

```
0100
```

Answer:

```
4
```

Correct.

---

## Example 2

Find:

```
10 - 6
```

---

### Binary

```
10 = 1010
```

```
6 = 0110
```

---

### 2's Complement of 6

```
0110
```

```
↓
```

1001

↓

1010

---

## Add

1010

+

1010

-----

10100

Discard Carry

0100

Answer:

4

---

## Hardware Representation

```
      A
      |
      |
      V
      +-----+
      | Adder  |
      +-----+
      ^
      |
      |
      2's Complement(B)
      |
```

V

Result

---

# Advantages of 2's Complement

## 1. Easy Representation

Negative numbers easily represent hote hain.

---

## 2. Simplifies Subtraction

Subtraction addition me convert ho jati hai.

---

## 3. Single Arithmetic Circuit

Same hardware use hota hai.

---

## 4. Fast Processing

Computer speed improve hoti hai.

---

## 5. No Separate Sign Handling

Sign automatically handle ho jata hai.

---

# Disadvantages

## 1. Concept Difficult for Beginners

Initial understanding difficult ho sakti hai.

---

## **2. Fixed Range**

Bit length ke according range limited hoti hai.

---

# **Applications**

### **CPU Arithmetic**

Addition and subtraction.

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### **ALU Design**

Arithmetic circuits.

---

### **Digital Computers**

Negative number representation.

---

### **Embedded Systems**

Microcontrollers.

---

### **Signal Processing**

DSP applications.

---

# **1's Complement vs 2's Complement**

| <b>1's Complement</b> | <b>2's Complement</b> |
|-----------------------|-----------------------|
| Bits Inverted         | 1's Complement + 1    |
| Two Zeros Possible    | Single Zero           |
| Complex Arithmetic    | Simple Arithmetic     |
| Less Efficient        | More Efficient        |
| Rarely Used           | Widely Used           |

## Viva Questions

### Q1. What is 2's Complement?

Method of representing negative binary numbers.

---

### Q2. How is 2's Complement obtained?

1's Complement + 1

---

### Q3. Why is 2's Complement used?

To represent negative numbers and simplify subtraction.

---

### Q4. What is the range of 8-bit 2's Complement?

-128 to +127

---

### Q5. Which complement is most commonly used?

2's Complement.

---

# Frequently Asked RGPV Questions

## 2 Marks

1. Define 2's Complement.
  2. How is 2's Complement obtained?
  3. What is 1's Complement?
  4. Why is 2's Complement used?
- 

## 5 Marks

1. Explain 2's Complement Representation.
  2. Explain method of finding 2's Complement.
  3. Compare 1's and 2's Complement.
- 

## 7 Marks

1. Explain 2's Complement with examples.
  2. Explain subtraction using 2's Complement.
  3. Discuss advantages of 2's Complement.
- 

## 14 Marks

1. Explain 2's Complement Representation with suitable examples.
  2. Discuss subtraction using 2's Complement method.
  3. Compare 1's Complement and 2's Complement and explain their applications.
- 

## PYQ Trend Analysis

| Topic                            | Frequency |
|----------------------------------|-----------|
| 2's Complement Basics            | ★★★★★     |
| Numerical Problems               | ★★★★★     |
| Subtraction Using 2's Complement | ★★★★★     |
| 1's vs 2's Complement            | ★★★★      |

## Expected 2026 Questions

- 🔥 Explain 2's Complement Representation with examples.
- 🔥 Perform subtraction using 2's Complement.
- 🔥 Compare 1's Complement and 2's Complement.
- 🔥 Explain advantages of 2's Complement.

## One-Minute Revision

- ✅ 2's Complement = 1's Complement + 1
- ✅ Negative numbers represented using 2's Complement
- ✅ Formula:

$$A - B = A + 2's \text{ Complement}(B)$$

- ✅ 8-bit Range:

-128 to +127

- ✅ Most commonly used representation method

# Conclusion

2's Complement Representation computer arithmetic me negative numbers ko represent karne ki sabse efficient technique hai. Iski madad se subtraction ko addition me convert kiya ja sakta hai aur hardware design simplify ho jata hai. Fast processing, simple arithmetic aur efficient representation ke karan ye modern computer systems me sabse adhik use kiya jata hai. 🎯

## Signed Addition and Subtraction

★★★★★ Most Important Topic

RGPV me Signed Addition & Subtraction se theory aur numerical dono puchhe jaate hain.

Booth Algorithm aur Floating Point samajhne ke liye bhi ye topic important hai.

Ye answer 3–4 pages aasani se cover karega.

---

## Signed Addition and Subtraction

### Introduction

Computer me numbers do types ke hote hain:

#### 1. Unsigned Numbers

Sirf positive numbers represent karte hain.

Example:

5, 10, 25

---

## 2. Signed Numbers

Positive aur Negative dono numbers represent karte hain.

Example:

+5, -5, +10, -10

Signed arithmetic me sign bit ka use hota hai.

---

## Definition

**"Signed Addition and Subtraction are arithmetic operations performed on positive and negative binary numbers using sign representation methods such as 2's Complement."**

---

## Sign Bit Representation

Most Significant Bit (MSB) sign ko represent karti hai.

| MSB | Meaning         |
|-----|-----------------|
| 0   | Positive Number |
| 1   | Negative Number |

---

## Examples

### Positive Number

+5

00000101

MSB = 0

---

## Negative Number

-5

11111011

MSB = 1

---

## Need of Signed Arithmetic

Signed arithmetic ka use:

- Banking Calculations
- Scientific Computing
- Engineering Applications
- Computer Programming
- Digital Signal Processing

me hota hai.

---

## Rules of Signed Addition

Signed Addition ke 4 possible cases hote hain.

---

### Case 1: Positive + Positive

#### Example

+5 + +3

Binary:

```
00000101
+
00000011
-----
00001000
```

Answer:

```
+8
```

---

## Rule

Signs same hain.

Simply add kar do.

Result positive hoga.

---

## Case 2: Negative + Negative

### Example

```
-5 + -3
```

---

### Binary Representation

```
-5 = 1111011
```

```
-3 = 1111101
```

Addition:

```
1111011
+
1111101
```

```
-----  
11111000
```

Result:

```
-8
```

---

## Rule

Signs same hain.

Numbers add karo.

Result negative hoga.

---

## Case 3: Positive + Negative

### Example

```
+8 + (-3)
```

---

### Binary

```
+8 = 00001000
```

```
-3 = 11111101
```

Addition:

```
00001000  
+  
11111101  
-----  
00000101
```

Answer:

+5

---

## Rule

Signs different hain.

Smaller number ko larger number se subtract karo.

Result larger number ke sign ka hoga.

---

## Case 4: Negative + Positive

### Example

-8 + 3

Result:

-5

---

## Rule

Same as Case-3

---

## Signed Subtraction

### Formula

Subtraction ko addition me convert karte hain.

$A - B$

$=$

$A + (2\text{'s Complement of } B)$

---

## Example 1

Find:

$7 - 3$

---

### Binary

$7 = 0111$

$3 = 0011$

---

### 2's Complement of 3

0011

↓

1100

↓

1101

---

### Addition

0111

+

1101

-----  
10100

Discard Carry

0100

Answer:

4

---

## Example 2

Find:

5 - 8

---

### Binary

5 = 0101

8 = 1000

---

### 2's Complement of 8

1000

↓

0111

↓

1000

---

### Addition

```
0101
+
1000
-----
1101
```

Result:

```
-3
```

---

## Overflow in Signed Arithmetic

### Definition

Overflow tab hota hai jab result available bits me represent nahi ho sakta.

---

### Example

4-bit Representation

```
0111
+
0001
-----
1000
```

Expected:

```
7 + 1 = 8
```

Lekin 4-bit signed range exceed ho gayi.

Overflow occur hua.

---

# Overflow Detection Rules

**Positive + Positive = Negative**

Overflow

---

**Negative + Negative = Positive**

Overflow

---

**Positive + Negative**

No Overflow

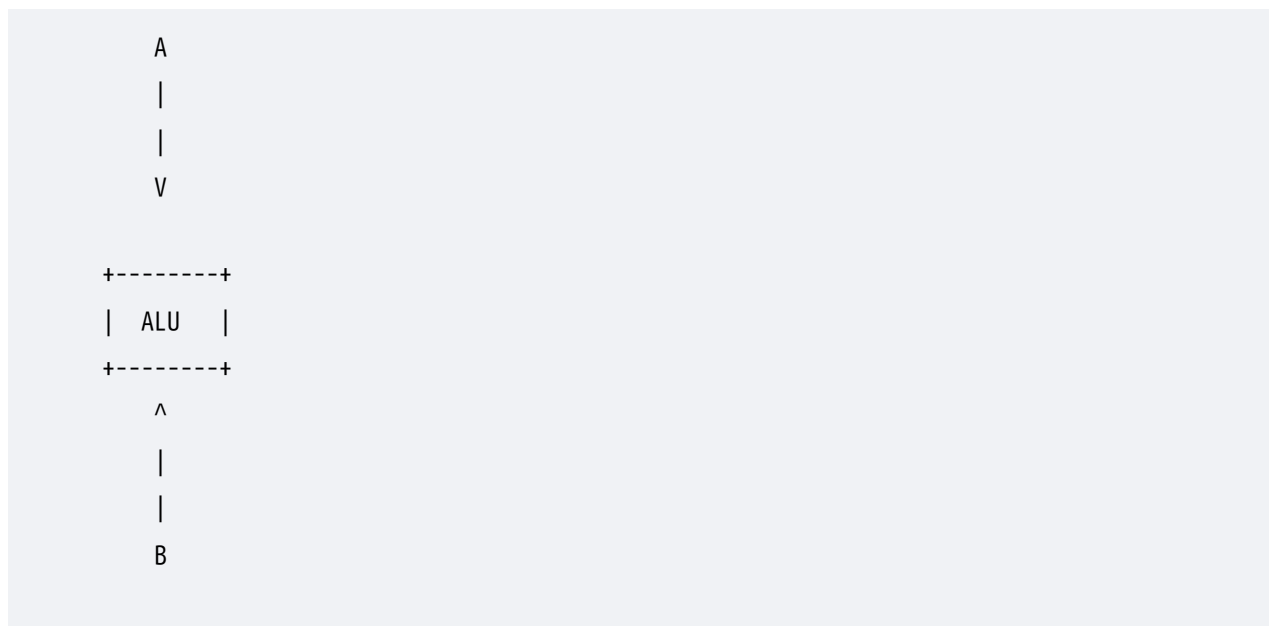
---

## Hardware for Signed Arithmetic

Signed arithmetic ALU ke through perform hota hai.

---

## Block Diagram



I  
V  
Result

---

## Steps of Signed Addition

Load Operand A



Load Operand B



Check Sign Bits



Perform Addition



Check Overflow



Store Result

---

## Steps of Signed Subtraction

Load A



Find 2's Complement of B



Add  $A + (-B)$



Check Overflow



# Advantages of Signed Arithmetic

## 1. Supports Negative Numbers

Negative values represent kar sakte hain.

---

## 2. Simplifies Calculations

Subtraction addition me convert ho jati hai.

---

## 3. Efficient Hardware

Same circuit use hota hai.

---

## 4. Fast Processing

CPU operations fast ho jati hain.

---

## 5. Useful in Real Applications

Scientific aur engineering calculations.

---

# Disadvantages

## 1. Overflow Problem

Large values par overflow ho sakta hai.

---

## 2. Complex for Beginners

Sign handling difficult lag sakta hai.

---

# Applications

## Banking Systems

Profit/Loss calculations.

---

## Scientific Computing

Positive & Negative values.

---

## Signal Processing

Wave calculations.

---

## Embedded Systems

Microcontroller arithmetic.

---

## Computer Graphics

Coordinate calculations.

---

# Signed vs Unsigned Numbers

| Signed Numbers      | Unsigned Numbers |
|---------------------|------------------|
| Positive & Negative | Only Positive    |

|                        |                       |
|------------------------|-----------------------|
| Uses Sign Bit          | No Sign Bit           |
| Smaller Positive Range | Larger Positive Range |
| More Flexible          | Simpler               |

---

## Viva Questions

### Q1. What is a Signed Number?

Number having a sign bit.

---

### Q2. What is MSB?

Most Significant Bit.

---

### Q3. What does MSB = 1 indicate?

Negative Number.

---

### Q4. What is Overflow?

Condition when result exceeds available bits.

---

### Q5. How is subtraction performed?

Using 2's Complement.

---

## Frequently Asked RGPV Questions

### 2 Marks

1. Define Signed Number.
  2. What is Sign Bit?
  3. What is Overflow?
  4. Define Signed Arithmetic.
- 

## 5 Marks

1. Explain Signed Addition.
  2. Explain Signed Subtraction.
  3. Explain Overflow.
- 

## 7 Marks

1. Explain Signed Addition with examples.
  2. Explain Signed Subtraction using 2's Complement.
  3. Explain Overflow Detection.
- 

## 14 Marks

1. Explain Signed Addition and Signed Subtraction with suitable examples.
  2. Discuss overflow in signed arithmetic.
  3. Explain arithmetic operations on signed numbers using 2's Complement.
- 

## PYQ Trend Analysis

| Topic              | Frequency |
|--------------------|-----------|
| Signed Addition    | ★★★★★     |
| Signed Subtraction | ★★★★★     |
| Overflow           | ★★★★      |

## Expected 2026 Questions

- 🔥 Explain Signed Addition with examples.
- 🔥 Explain Signed Subtraction using 2's Complement.
- 🔥 Explain Overflow and its detection.
- 🔥 Perform signed arithmetic numericals.

## One-Minute Revision

- ✅ MSB = Sign Bit

0 → Positive

1 → Negative

- ✅ Same Signs → Add
- ✅ Different Signs → Subtract

- ✅ Subtraction:

$A - B$

=

$A + 2\text{'s Complement}(B)$

- ✅ Overflow:

$(+)(+) = (-)$

or

$$(-)+(-) = (+)$$

---

## Conclusion

Signed Addition and Subtraction computer arithmetic ke important operations hain jo positive aur negative binary numbers par perform kiye jate hain. 2's Complement representation aur ALU ki madad se ye operations efficiently execute hote hain. Overflow detection aur sign-bit handling is topic ke key concepts hain. Ye RGPV exams ka highly important numerical aur theory topic hai.



## Multiplication and Division

★★★★★ Most Important Topic

RGPV me Multiplication, Division aur Booth Algorithm ek hi unit ke most scoring topics hain.

Theory + Numerical dono puchhe ja sakte hain.

Ye answer **3–4 pages** aasani se cover karega.

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## Multiplication and Division

### Introduction

Computer Arithmetic me Multiplication aur Division do important arithmetic operations hain.

Computer directly decimal numbers par kaam nahi karta. Isliye ye operations binary numbers par perform kiye jaate hain.

ALU (Arithmetic Logic Unit) multiplication aur division operations ko execute karta hai.

---

## Definition

### Binary Multiplication

**"Binary Multiplication is the process of multiplying two binary numbers using binary arithmetic rules."**

### Binary Division

**"Binary Division is the process of dividing one binary number by another binary number using binary arithmetic rules."**

---

## Need of Multiplication and Division

Multiplication aur Division ka use:

- Scientific Calculations
- Banking Systems
- Engineering Applications
- Computer Graphics
- Digital Signal Processing

me hota hai.

---

## Binary Multiplication

Binary multiplication decimal multiplication ki tarah hi hoti hai.

---

# Rules of Binary Multiplication

| A | B | Result |
|---|---|--------|
| 0 | 0 | 0      |
| 0 | 1 | 0      |
| 1 | 0 | 0      |
| 1 | 1 | 1      |

## Important Rule

$$1 \times 1 = 1$$

## Example 1

Multiply:

$$\begin{array}{r} 101 \\ \times 11 \\ \hline \end{array}$$

### Step 1

$$\begin{array}{r} 101 \\ \times 011 \\ \hline 101 \\ + 1010 \\ \hline 1111 \end{array}$$

## Verification

$$101_2 = 5$$

$$11_2 = 3$$

Result:

$$1111_2 = 15$$

Therefore:

$$5 \times 3 = 15$$

Correct.

---

## Example 2

Multiply:

$$\begin{array}{r} 110 \\ \times 10 \\ \hline \end{array}$$

## Solution

$$\begin{array}{r} 110 \\ \times 10 \\ \hline 000 \\ + 1100 \\ \hline 1100 \end{array}$$

## Verification

$$110_2 = 6$$

$$10_2 = 2$$

$$6 \times 2 = 12$$

$$1100_2 = 12$$

Correct.

---

## Hardware Multiplication Process

Multiplicand

|  
V

Multiplier

|  
V

Shift & Add

|  
V

Product

---

## Steps of Binary Multiplication

### Step 1

Take Multiplicand.

---

### Step 2

Take Multiplier.

---

### **Step 3**

Check multiplier bit.

---

### **Step 4**

If bit = 1 → Add

If bit = 0 → Ignore

---

### **Step 5**

Shift left.

---

### **Step 6**

Repeat until all bits processed.

---

## **Advantages of Binary Multiplication**

### **1. Simple Logic**

Easy hardware implementation.

---

### **2. Fast Processing**

Efficient ALU operations.

---

### **3. Suitable for Digital Systems**

Used in processors.

---

# Binary Division

Binary Division decimal division ke similar hoti hai.

---

## Terms Used

Dividend ÷ Divisor

---

## Example

1010 ÷ 10

---

## Binary Division Rules

| A     | B            | Result |
|-------|--------------|--------|
| 0 ÷ 1 | 0            |        |
| 1 ÷ 1 | 1            |        |
| 0 ÷ 0 | Undefined    |        |
| 1 ÷ 0 | Not Possible |        |

---

## Example 1

Divide:

1010 ÷ 10

---

## Solution

$$\begin{array}{r}
 101 \\
 \text{-----} \\
 10 \ ) \ 1010 \\
 \phantom{10} 10 \\
 \text{----} \\
 \phantom{10} 001
 \end{array}$$


---

## Verification

$$1010_2 = 10$$

$$10_2 = 2$$

$$10 \div 2 = 5$$

$$101_2 = 5$$

Correct.

---

## Example 2

Divide:

$$1100 \div 10$$


---

## Solution

$$\begin{array}{r}
 110 \\
 \text{-----} \\
 10 \ ) \ 1100 \\
 \phantom{10} 10 \\
 \text{----} \\
 \phantom{10} 100 \\
 \phantom{10} 10 \\
 \text{---} \\
 \phantom{10} 00
 \end{array}$$

Answer:

$110_2$

---

## Verification

$$12 \div 2 = 6$$

Correct.

---

# Hardware Division Process

Dividend

|

v

Divisor

|

v

Compare

Subtract

Shift

|

v

Quotient

---

# Division Algorithm

## Step 1

Load Dividend.

---

## Step 2

Load Divisor.

---

## Step 3

Compare Divisor and Dividend.

---

## Step 4

Subtract Divisor.

---

## Step 5

Generate Quotient Bit.

---

## Step 6

Repeat until completion.

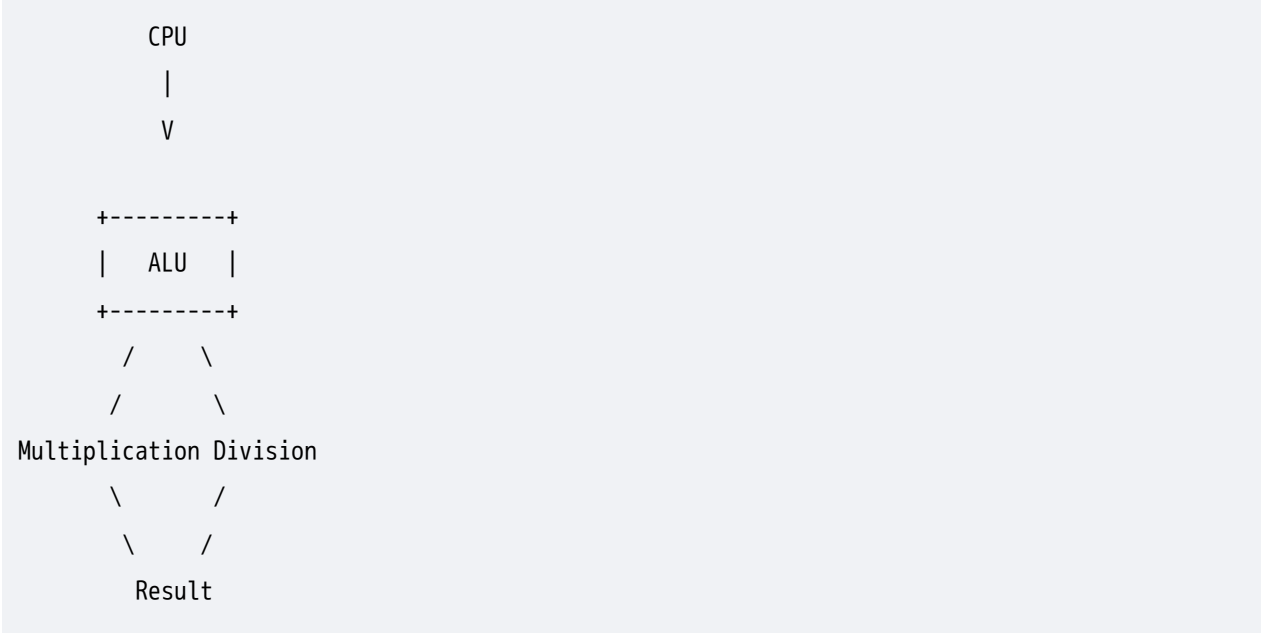
---

# Multiplication vs Division

| Multiplication        | Division             |
|-----------------------|----------------------|
| Repeated Addition     | Repeated Subtraction |
| Product Obtained      | Quotient Obtained    |
| Faster                | Comparatively Slower |
| Shift Left Used       | Shift Right Used     |
| Example: $5 \times 3$ | Example: $15 \div 3$ |

---

# Hardware Block Diagram



## Applications

### Scientific Computing

Complex calculations.

---

### Computer Graphics

Image processing.

---

### Banking Systems

Interest calculations.

---

### Digital Signal Processing

Signal operations.

---

## **Embedded Systems**

Microcontroller calculations.

---

# **Advantages**

### **1. Fast Computation**

Complex calculations quickly perform hoti hain.

---

### **2. High Accuracy**

Binary arithmetic errors kam hote hain.

---

### **3. Efficient Hardware**

ALU implementation easy hoti hai.

---

### **4. Essential for Modern Computing**

Almost every application me use hota hai.

---

# **Disadvantages**

### **1. Large Binary Numbers**

Manual calculations difficult.

---

### **2. Division Slower Than Addition**

More clock cycles lagte hain.

---

### 3. Hardware Complexity

Advanced multiplication circuits complex hote hain.

---

## Viva Questions

### Q1. What is Binary Multiplication?

Multiplication of two binary numbers.

---

### Q2. What is Binary Division?

Division of one binary number by another.

---

### Q3. Which unit performs multiplication?

ALU.

---

### Q4. Which operation is slower?

Division.

---

### Q5. What is Product?

Result of multiplication.

---

## Frequently Asked RGPV Questions

### 2 Marks

1. Define Binary Multiplication.

2. Define Binary Division.
  3. What is Product?
  4. What is Quotient?
- 

## 5 Marks

1. Explain Binary Multiplication.
  2. Explain Binary Division.
  3. Write multiplication rules.
- 

## 7 Marks

1. Explain multiplication with example.
  2. Explain division with example.
  3. Compare multiplication and division.
- 

## 14 Marks

1. Explain Binary Multiplication and Binary Division with suitable examples.
  2. Discuss multiplication and division operations in computer arithmetic.
  3. Explain hardware implementation of multiplication and division.
- 

## PYQ Trend Analysis

| Topic                 | Frequency |
|-----------------------|-----------|
| Binary Multiplication | ★★★★★     |
| Binary Division       | ★★★★★     |
| Numerical Problems    | ★★★★★     |

## Expected 2026 Questions

- 🔥 Explain Binary Multiplication with example.
- 🔥 Explain Binary Division with example.
- 🔥 Compare Multiplication and Division.
- 🔥 Discuss arithmetic operations performed by ALU.

## One-Minute Revision

- ✓ Multiplication = Repeated Addition
- ✓ Division = Repeated Subtraction
- ✓ Rule:

$$1 \times 1 = 1$$

- ✓ Product = Multiplication Result
- ✓ Quotient = Division Result
- ✓ ALU performs both operations

## Conclusion

Multiplication and Division computer arithmetic ke fundamental operations hain jo binary numbers par perform kiye jate hain. ALU in operations ko execute karta hai aur shift-add aur

repeated subtraction techniques ki madad se results generate karta hai. Ye Computer Organization ka important aur frequently asked topic hai aur numericals ke liye bhi bahut scoring hai. 🎯

## Booth's Algorithm

★★★★★ Most Important & Most Repeated Numerical Topic

RGPV me Booth's Algorithm se direct **7 marks**, **10 marks** aur **14 marks** ke questions aate hain.

Exam me numerical solve karne ke chances bahut high hote hain.

Ye answer **4–5 pages** aasani se cover karega.

---

## Booth's Algorithm

### Introduction

Computer me signed binary numbers ka multiplication karna normal multiplication se thoda difficult hota hai.

Is problem ko solve karne ke liye **Andrew D. Booth** ne Booth's Algorithm diya tha.

Booth's Algorithm signed positive aur signed negative binary numbers ke multiplication ke liye use kiya jata hai.

---

### Definition

"Booth's Algorithm is an efficient multiplication algorithm used for multiplying signed binary numbers in 2's complement form."

---

## Need of Booth's Algorithm

### 1. Signed Number Multiplication

Positive aur Negative dono numbers multiply kar sakta hai.

### 2. Fast Computation

Number of additions reduce karta hai.

### 3. Efficient Hardware

Processor implementation easy hoti hai.

### 4. Used in ALU

Modern processors me use hota hai.

---

## Basic Principle

Booth's Algorithm multiplier ke consecutive bits ko observe karta hai.

Hum do bits check karte hain:

Q0 Q-1

---

## Decision Table

| Q0 | Q-1 | Operation |
|----|-----|-----------|
|----|-----|-----------|

|   |   |                           |
|---|---|---------------------------|
| 0 | 0 | No Operation              |
| 1 | 1 | No Operation              |
| 0 | 1 | Add Multiplicand (M)      |
| 1 | 0 | Subtract Multiplicand (M) |

## Registers Used

### M

Multiplicand

---

### Q

Multiplier

---

### A

Accumulator

---

### Q-1

Extra Bit

---

### Count

Number of bits

---

# Booth's Algorithm Flow

Initialize Registers



Check  $Q_0$  and  $Q_{-1}$



Add/Subtract M



Arithmetic Right Shift



Count - 1



Repeat



Final Product

## Algorithm Steps

### Step 1

Initialize:

A = 0000

Q = Multiplier

M = Multiplicand

$Q_{-1} = 0$

### Step 2

Check:

$Q_0$  and  $Q_{-1}$

### Step 3

Apply Rule

| Q0Q-1 | Operation   |
|-------|-------------|
| 00    | Nothing     |
| 11    | Nothing     |
| 01    | $A = A + M$ |
| 10    | $A = A - M$ |

### Step 4

Arithmetic Right Shift

(A, Q, Q-1)

### Step 5

Count Reduce

### Step 6

Repeat Until Count = 0

## Numerical Example

**Multiply:**

$5 \times 3$

# Binary Representation

M = 0101

Q = 0011

A = 0000

Q-1 = 0

Count = 4

---

## Step-1

Current:

A = 0000

Q = 0011

Q-1 = 0

Check:

Q0Q-1

1 0

Rule:

$10 \rightarrow A = A - M$

---

A:

0000

-

0101

=

1011

---

Arithmetic Right Shift

A = 1101

Q = 1001

Q-1 = 1

---

## Step-2

Check:

QQQ-1

1 1

No Operation

Shift

A = 1110

Q = 1100

Q-1 = 1

---

## Step-3

Check:

Q0Q-1

0 1

Rule:

$01 \rightarrow A = A + M$

Addition:

1110

+

0101

=

0011

Shift

A = 0001

Q = 1110

Q-1 = 0

---

## Step-4

Check:

Q0Q-1

0 0

No Operation

Shift

A = 0000

Q = 1111

---

## Final Result

AQ

00001111

Decimal:

15

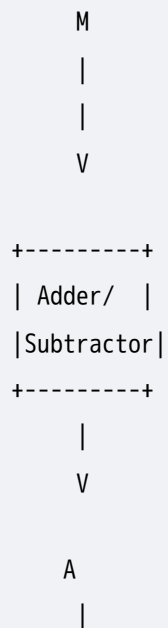
Hence:

$5 \times 3 = 15$

Correct.

---

## Hardware Block Diagram



|  
V  
  
Q  
|  
|  
Q-1

---

## Arithmetic Right Shift

Most Important Concept

Example:

Before Shift

A = 1010

Q = 1100

Q-1 = 1

After Shift

A = 1101

Q = 0110

Q-1 = 0

Sign bit preserve hoti hai.

---

## Advantages of Booth's Algorithm

### 1. Signed Multiplication

Positive aur negative dono handle karta hai.

---

## **2. Fast Processing**

Additions reduce hoti hain.

---

## **3. Efficient Hardware**

ALU implementation easy.

---

## **4. Reduced Computation**

Less arithmetic operations.

---

## **5. Widely Used**

Modern processors me use hota hai.

---

# **Disadvantages**

## **1. Complex Algorithm**

Normal multiplication se difficult.

---

## **2. Shift Operations Required**

Extra hardware lag sakta hai.

---

## **3. Difficult Manual Calculation**

Exam me mistakes ho sakti hain.

---

# Applications

## CPU Design

Processor multiplication unit.

---

## Digital Signal Processing

DSP calculations.

---

## Scientific Computing

Fast arithmetic.

---

## Embedded Systems

Microcontrollers.

---

## Computer Architecture

Signed arithmetic operations.

---

# Booth's Algorithm vs Ordinary Multiplication

| Booth Algorithm | Ordinary Multiplication |
|-----------------|-------------------------|
| Signed Numbers  | Mostly Unsigned         |
| Faster          | Slower                  |
| Less Additions  | More Additions          |
| Uses Shifting   | Simple Multiplication   |

|                    |                |
|--------------------|----------------|
| Hardware Efficient | Less Efficient |
|--------------------|----------------|

---

## Viva Questions

### Q1. What is Booth's Algorithm?

Algorithm used for signed binary multiplication.

---

### Q2. Who proposed Booth's Algorithm?

Andrew D. Booth.

---

### Q3. Which representation is used?

2's Complement.

---

### Q4. Why is Q-1 used?

To determine operation.

---

### Q5. Which shift is used?

Arithmetic Right Shift.

---

## Frequently Asked RGPV Questions

### 2 Marks

1. Define Booth's Algorithm.
2. What is Arithmetic Right Shift?
3. What is Q-1?

4. Why is Booth's Algorithm used?

---

## 5 Marks

1. Explain Booth's Algorithm.
  2. Explain Arithmetic Right Shift.
  3. Write decision table of Booth's Algorithm.
- 

## 7 Marks

1. Explain Booth's Algorithm with flowchart.
  2. Perform multiplication using Booth's Algorithm.
  3. Explain registers used in Booth's Algorithm.
- 

## 14 Marks

1. Explain Booth's Algorithm with suitable numerical example.
  2. Discuss signed binary multiplication using Booth's Algorithm.
  3. Explain Booth's Algorithm with block diagram and working.
- 

## PYQ Trend Analysis

| Topic                  | Frequency |
|------------------------|-----------|
| Booth Algorithm Theory | ★★★★★     |
| Numerical Problems     | ★★★★★     |
| Arithmetic Right Shift | ★★★★★     |
| Decision Table         | ★★★★★     |

---

# Expected 2026 Questions

- 🔥 Explain Booth's Algorithm with numerical example.
  - 🔥 Perform signed multiplication using Booth's Algorithm.
  - 🔥 Explain Arithmetic Right Shift in Booth's Algorithm.
  - 🔥 Discuss advantages of Booth's Algorithm.
- 

## One-Minute Revision

- ✓ Used for Signed Multiplication
- ✓ Uses 2's Complement
- ✓ Registers:

A  
Q  
M  
Q-1

- ✓ Rules:

| Q0Q-1 | Action     |
|-------|------------|
| 00    | Nothing    |
| 11    | Nothing    |
| 01    | Add M      |
| 10    | Subtract M |

✓ Arithmetic Right Shift after every step

---

## Conclusion

Booth's Algorithm signed binary multiplication ke liye ek efficient technique hai jo 2's Complement representation aur Arithmetic Right Shift ka use karti hai. Ye multiplication process ko fast aur hardware-efficient banati hai. Computer Architecture, ALU design aur modern processors me iska bahut important role hai. RGPV exams me ye sabse important numerical topics me se ek hai. 🎯

## Floating Point Arithmetic Operation

★★★★★ Most Important Topic

RGPV me Floating Point Representation aur Floating Point Arithmetic se theory + numerical dono puchhe jate hain.

Ye topic computer me **very large aur very small numbers** represent karne ke liye use hota hai.

Ye answer **4–5 pages** aasani se cover karega.

---

## Floating Point Arithmetic Operation

### Introduction

Computer me kai baar bahut bade numbers aur bahut chhote decimal numbers ke saath calculations karni padti hain.

Example:

```
125000000
```

```
0.000000125
```

In numbers ko normal binary representation me store karna difficult hota hai.

Isliye Floating Point Representation ka use kiya jata hai.

---

## Definition

**"Floating Point Arithmetic is a method of representing and performing arithmetic operations on real numbers using a mantissa and exponent."**

---

## Scientific Notation Concept

Floating Point Representation scientific notation par based hoti hai.

### Example

Decimal Number:

```
125000
```

Scientific Notation:

```
1.25 × 105
```

---

### Example

0.000125

Scientific Notation:

$1.25 \times 10^{-4}$

---

# Floating Point Representation

Floating Point Number ke three parts hote hain:

-----  
| Sign | Exponent | Mantissa |  
-----

---

## 1. Sign Bit

Number positive hai ya negative.

0 = Positive

1 = Negative

---

## 2. Exponent

Decimal point ki position batata hai.

---

## 3. Mantissa

Actual significant digits store karta hai.

---

## Example

Number:

13.25

Binary:

1101.01

Normalize:

$1.10101 \times 2^3$

---

## Components

Sign = 0

Exponent = 3

Mantissa = 10101

---

## Floating Point Format

### 32-bit IEEE 754 Format

Most Important

-----  
| Sign | Exponent | Mantissa |

-----  
| 1 bit | 8 bits | 23 bits |

---

## IEEE 754 Representation

## Sign Bit

1 Bit

---

## Exponent

8 Bits

---

## Fraction/Mantissa

23 Bits

---

## Diagram

-----  
| S | EEEEEEE | MMMMMMMMMMMMMMMMMMMMMMM |  
-----

---

## Example

+5.75

Binary:

101.11

Normalize:

$1.0111 \times 2^2$

---

Components:

Sign = 0

Exponent = 2

Mantissa = 0111

---

# Floating Point Addition

Most Important

---

## Steps

### Step 1

Equalize Exponents

---

### Step 2

Add Mantissas

---

### Step 3

Normalize Result

---

### Step 4

Adjust Exponent

---

## Example

Add:

$$1.5 \times 10^2$$

+

$$2.5 \times 10^2$$

---

Same exponent hai.

Add mantissa:

$$1.5 + 2.5$$

=

$$4.0$$

Result:

$$4.0 \times 10^2$$

---

## Floating Point Addition Flow

Align Exponents

↓

Add Mantissas

↓

Normalize

↓

Store Result

---

## Floating Point Subtraction

### Steps

#### Step 1

Equalize Exponents

## Step 2

Subtract Mantissas

## Step 3

Normalize Result

## Step 4

Store Result

---

# Example

$$5.5 \times 10^2$$

-

$$2.5 \times 10^2$$

---

Subtract:

$$5.5 - 2.5$$

=

$$3.0$$

Result:

$$3.0 \times 10^2$$

---

# Floating Point Multiplication

Most Important

---

## Rule

**Multiply Mantissas**

**Add Exponents**

---

## Formula

$$(M1 \times 2^{E1})$$
$$\times$$
$$(M2 \times 2^{E2})$$
$$=$$
$$(M1 \times M2)$$
$$\times$$
$$2^{(E1+E2)}$$

---

## Example

$$1.5 \times 10^2$$
$$\times$$
$$2.0 \times 10^3$$

---

Mantissa:

$1.5 \times 2.0$

=

$3.0$

---

Exponent:

$2 + 3$

=

$5$

---

Result:

$3.0 \times 10^5$

---

## Floating Point Division

Most Important

---

### Rule

**Divide Mantissas**

**Subtract Exponents**

---

### Formula

$(M1 \times 2E1)$

$\div$

$$(M_2 \times 2E_2)$$

=

$$(M_1 \div M_2)$$

×

$$2(E_1 - E_2)$$

## Example

$$8 \times 10^5$$

÷

$$2 \times 10^2$$

Mantissa:

$$8 \div 2$$

=

$$4$$

Exponent:

$$5 - 2$$

=

$$3$$

Result:

$$4 \times 10^3$$

# Normalization

Most Important Concept

---

## Definition

Floating point number ko standard form me convert karna.

---

## Example

101.01

Normalize:

$1.0101 \times 2^2$

---

# Overflow

## Definition

Jab exponent maximum limit se exceed ho jaye.

---

## Example

Very large number:

$10^{300}$

Overflow generate kar sakta hai.

---

# Underflow

## Definition

Jab exponent bahut chhota ho jaye.

---

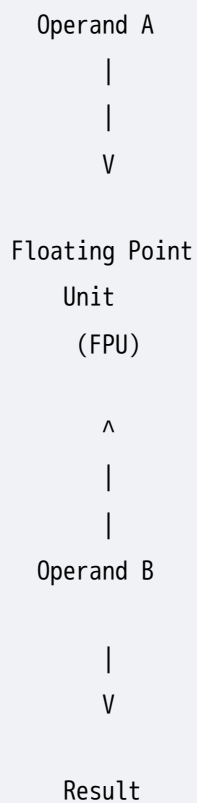
## Example

$10^{-300}$

Underflow generate kar sakta hai.

---

# Hardware for Floating Point Arithmetic



# Floating Point Unit (FPU)

## Definition

Special hardware unit jo floating point operations perform karti hai.

---

## Functions

- Addition
  - Subtraction
  - Multiplication
  - Division
- 

## Advantages

### 1. Large Range

Bahut bade numbers represent kar sakta hai.

---

### 2. High Precision

Accurate calculations.

---

### 3. Scientific Applications

Engineering calculations ke liye suitable.

---

### 4. Fast Processing

Modern processors me dedicated FPU hota hai.

---

## **5. Real Number Support**

Decimal values represent kar sakta hai.

---

# **Disadvantages**

## **1. Complex Hardware**

Implementation difficult hoti hai.

---

## **2. Rounding Errors**

Precision loss ho sakti hai.

---

## **3. High Cost**

FPU design expensive hoti hai.

---

# **Applications**

## **Scientific Computing**

Physics simulations.

---

## **Engineering**

CAD/CAM systems.

---

# Artificial Intelligence

Machine Learning calculations.

---

# Computer Graphics

3D Rendering.

---

# Weather Forecasting

Complex mathematical models.

---

# Fixed Point vs Floating Point

| Fixed Point            | Floating Point            |
|------------------------|---------------------------|
| Decimal Position Fixed | Decimal Position Variable |
| Small Range            | Large Range               |
| Simple Hardware        | Complex Hardware          |
| Less Precision         | High Precision            |
| Faster                 | Slightly Slower           |

---

# Viva Questions

## Q1. What is Floating Point Arithmetic?

Arithmetic performed on real numbers using exponent and mantissa.

---

## Q2. What is Mantissa?

Significant digits of number.

---

### **Q3. What is Exponent?**

Position of decimal point.

---

### **Q4. What is IEEE 754?**

Standard floating point representation.

---

### **Q5. What is FPU?**

Floating Point Unit.

---

## **Frequently Asked RGPV Questions**

### **2 Marks**

1. Define Floating Point Representation.
  2. What is Mantissa?
  3. What is Exponent?
  4. What is FPU?
- 

### **5 Marks**

1. Explain Floating Point Representation.
  2. Explain IEEE 754 format.
  3. Explain Normalization.
- 

### **7 Marks**

1. Explain Floating Point Addition.
  2. Explain Floating Point Multiplication.
  3. Explain Overflow and Underflow.
- 

## 14 Marks





1. Explain Floating Point Arithmetic Operations with suitable examples.
  2. Discuss Floating Point Representation and IEEE 754 format.
  3. Explain Addition, Subtraction, Multiplication and Division in Floating Point Arithmetic.
- 

## PYQ Trend Analysis

| Topic                         | Frequency |
|-------------------------------|-----------|
| Floating Point Representation | ★★★★★     |
| IEEE 754 Format               | ★★★★★     |
| Floating Point Arithmetic     | ★★★★★     |
| Overflow/Underflow            | ★★★★      |
| Normalization                 | ★★★★      |

---

## Expected 2026 Questions

-  Explain Floating Point Arithmetic Operations.
  -  Explain IEEE 754 Floating Point Format.
  -  Explain Floating Point Addition and Multiplication.
  -  Explain Normalization, Overflow and Underflow.
-

# One-Minute Revision

✓ Floating Point Number:

Sign + Exponent + Mantissa

✓ IEEE 754:

1 Bit Sign

8 Bit Exponent

23 Bit Mantissa

✓ Multiplication:

Multiply Mantissa

Add Exponents

✓ Division:

Divide Mantissa

Subtract Exponents

✓ Used for Real Numbers

---

## Conclusion

Floating Point Arithmetic computer systems me real numbers ko represent aur process karne ki ek efficient technique hai. Isme Sign Bit, Exponent aur Mantissa ka use hota hai. IEEE 754 standard floating point representation ka widely used format hai. Floating Point Arithmetic scientific computing, AI, graphics aur engineering applications me bahut important role play karti hai aur RGPV exams ka highly important topic hai. 🎯

# Design of Arithmetic Unit

★★★★★ Most Important Topic

RGPV me "Design of Arithmetic Unit" se direct 7 marks aur 14 marks ke questions frequently puche jate hain.

Ye topic ALU, Adders aur Arithmetic Operations se directly related hai.

Ye answer 3–4 **pages** aasani se cover karega.

---

# Design of Arithmetic Unit

## Introduction

Computer me saare arithmetic operations jaise:

- Addition
- Subtraction
- Increment
- Decrement
- Transfer

ek special hardware unit dwara perform kiye jate hain jise **Arithmetic Unit** kehte hain.

Arithmetic Unit ALU (Arithmetic Logic Unit) ka important part hota hai.

---

## Definition

"Arithmetic Unit is a digital circuit that performs arithmetic operations on binary data under the control of selection inputs."

---

## Need of Arithmetic Unit

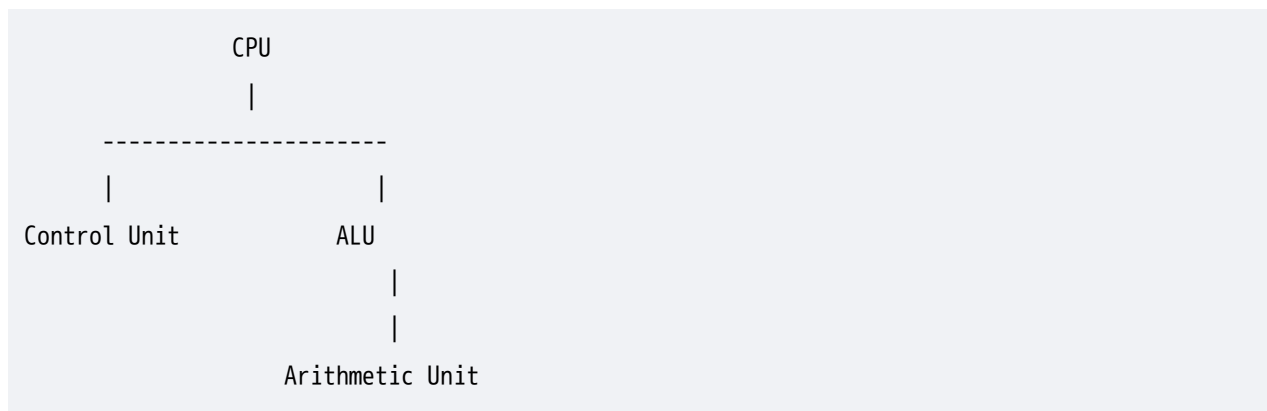
Arithmetic Unit ka use:

- ✓ Binary Addition
- ✓ Binary Subtraction
- ✓ Increment
- ✓ Decrement
- ✓ Data Transfer

ke liye hota hai.

---

## Arithmetic Unit in CPU



## Basic Components of Arithmetic Unit

Arithmetic Unit mainly following components se milkar banti hai:

## 1. Full Adder

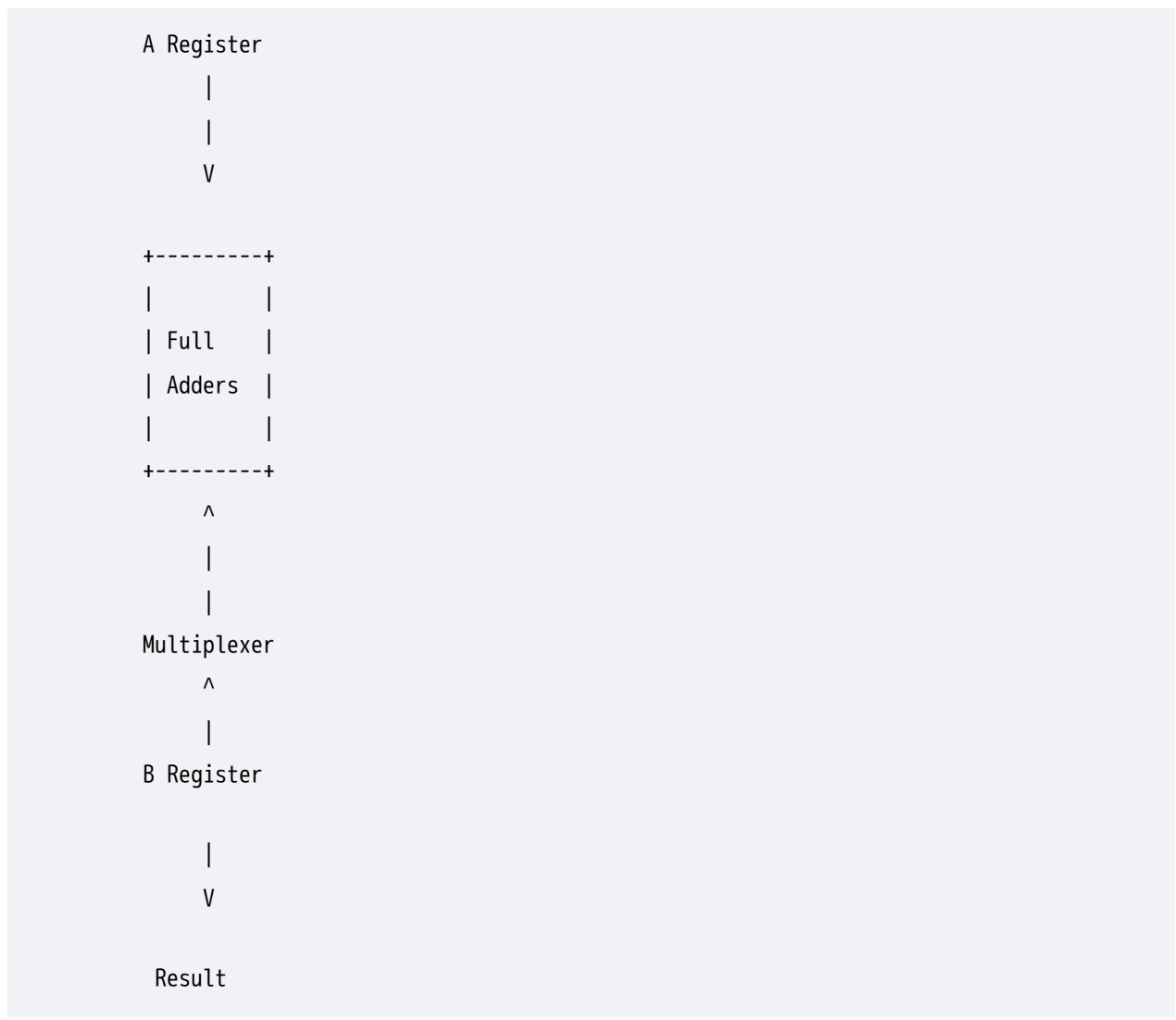
## 2. Multiplexer

## 3. Control Lines

## 4. Registers

---

# Block Diagram of Arithmetic Unit



---

## Working Principle

Arithmetic Unit do operands par operation perform karti hai.

Suppose:

A = Operand-1

B = Operand-2

Control Signals decide karte hain ki kaunsa operation perform hoga.

---

## Arithmetic Circuit

Arithmetic Unit ka main circuit Full Adders ka combination hota hai.

---

### 4-Bit Arithmetic Unit

```
A3 A2 A1 A0
|  |  |  |
-----
| Full Adders |
-----
|  |  |  |
F3 F2 F1 F0
```

## Selection Variables

Arithmetic Unit me generally:

S1

S0

Cin

use hote hain.

---

# Arithmetic Operations Table

| S1 | S0 | Cin | Operation      |
|----|----|-----|----------------|
| 0  | 0  | 0   | Transfer A     |
| 0  | 0  | 1   | Increment A    |
| 0  | 1  | 0   | Addition       |
| 0  | 1  | 1   | Add with Carry |
| 1  | 0  | 0   | Subtraction    |
| 1  | 0  | 1   | Decrement A    |
| 1  | 1  | 0   | Transfer B     |
| 1  | 1  | 1   | Increment B    |

★ Table exam me bahut important hai.

---

## Operation 1: Transfer

### RTL

$F \leftarrow A$

Meaning:

A ka data directly output me transfer hoga.

---

## Operation 2: Increment

## RTL

$F \leftarrow A + 1$

---

## Example

$A = 0101$

Result:

0110

---

## Operation 3: Addition

## RTL

$F \leftarrow A + B$

---

## Example

$A = 0101$

$B = 0011$

Result:

1000

Decimal:

$5 + 3 = 8$

---

# Operation 4: Add with Carry

## RTL

$$F \leftarrow A + B + C_{in}$$

---

## Example

$$5 + 3 + 1 = 9$$

---

# Operation 5: Subtraction

Most Important

---

## Formula

$$\begin{aligned} A - B \\ = \\ A + 2's \text{ Complement}(B) \end{aligned}$$

---

## Example

$$7 - 3$$

Binary:

0111

0011

2's Complement:

1101

Addition:

```
0111
+
1101
-----
0100
```

Answer:

4

---

## Operation 6: Decrement

### RTL

$F \leftarrow A - 1$

---

### Example

A = 0110

Result:

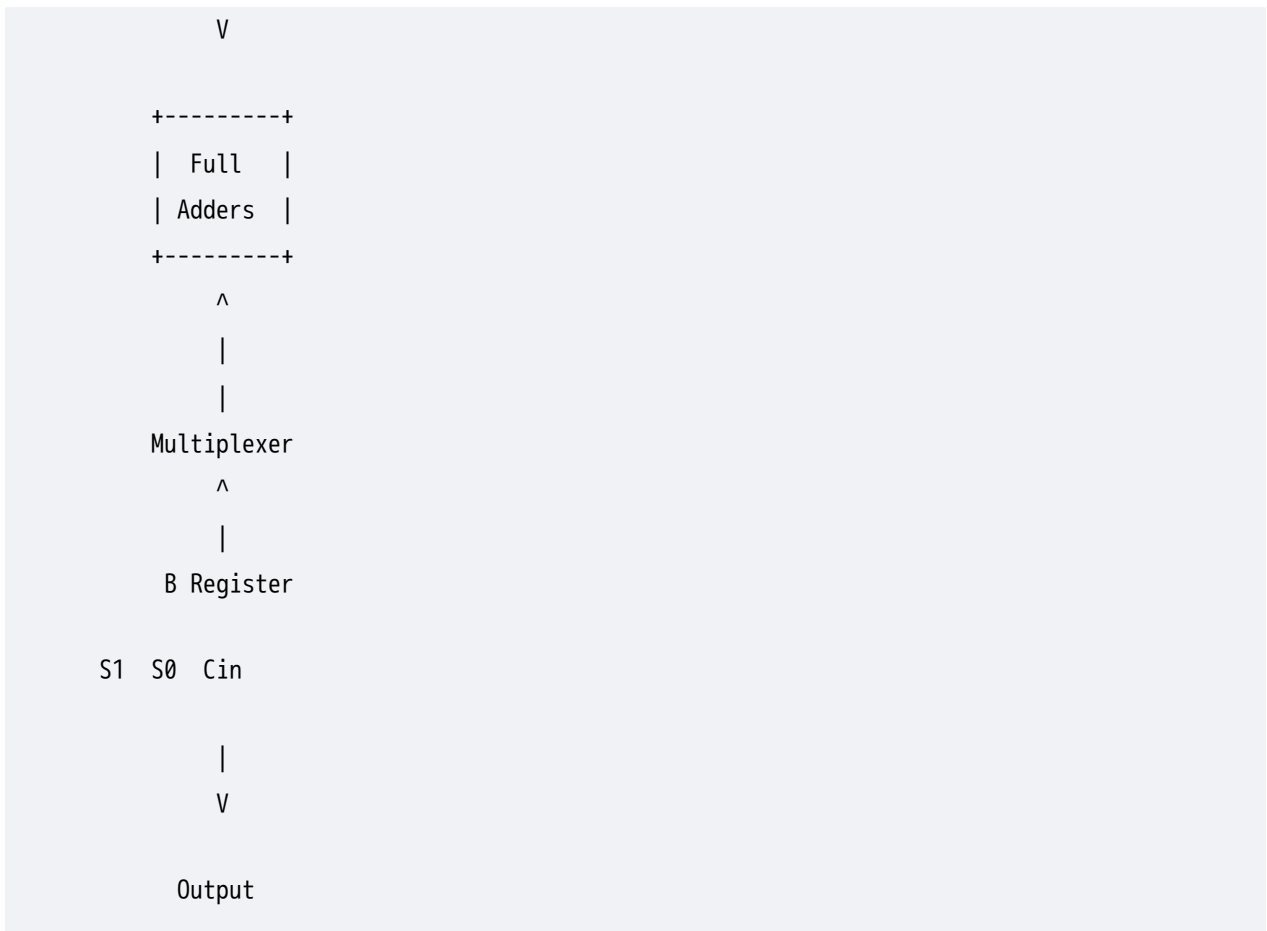
0101

---

## Hardware Design of Arithmetic Unit

A Register

|  
|



## Role of Multiplexer

Multiplexer arithmetic operation select karta hai.

Example:

$S1 = 0$

$S0 = 1$

Addition select ho sakta hai.

## Role of Full Adder

Full Adder perform karta hai:

$$A + B + C_{in}$$

Har bit ke liye ek Full Adder use hota hai.

---

## Advantages of Arithmetic Unit

### 1. Fast Calculations

High-speed arithmetic operations.

---

### 2. Hardware Efficient

Single circuit multiple operations perform karta hai.

---

### 3. Flexible

Different arithmetic functions perform kar sakta hai.

---

### 4. Used in ALU

CPU performance improve hoti hai.

---

### 5. Automatic Operation Selection

Control signals ke through.

---

## Disadvantages

### 1. Complex Circuit Design

Large bit-width par complexity badh jati hai.

---

## **2. Hardware Cost**

Advanced processors me cost increase hoti hai.

---

## **3. Power Consumption**

Large arithmetic units more power consume karti hain.

---

# **Applications**

## **CPUs**

Arithmetic calculations.

---

## **Microprocessors**

Data processing.

---

## **Digital Computers**

Basic arithmetic operations.

---

## **Embedded Systems**

Microcontroller calculations.

---

## **Scientific Computing**

Complex mathematical operations.

---

# **Arithmetic Unit vs ALU**

| <b>Arithmetic Unit</b>         | <b>ALU</b>                               |
|--------------------------------|--|
| Performs Arithmetic Operations | Performs Arithmetic + Logical Operations |
| Sub-part of ALU                | Complete Unit                            |
| Addition, Subtraction          | Addition, Subtraction, AND, OR, NOT      |
| Limited Functions              | More Functions                           |

## Viva Questions

### Q1. What is Arithmetic Unit?

Circuit used to perform arithmetic operations.

---

### Q2. What are the main components?

Full Adder and Multiplexer.

---

### Q3. Which unit performs subtraction?

Arithmetic Unit.

---

### Q4. Why is Multiplexer used?

To select arithmetic operations.

---

### Q5. Is Arithmetic Unit a part of ALU?

Yes.

---

## Frequently Asked RGPV Questions

## 2 Marks

1. Define Arithmetic Unit.
  2. What is the role of Full Adder?
  3. What is Multiplexer?
  4. What is Increment Operation?
- 

## 5 Marks

1. Explain Arithmetic Unit.
  2. Explain Arithmetic Operations.
  3. Explain role of Multiplexer.
- 

## 7 Marks

1. Explain Design of Arithmetic Unit.
  2. Explain Arithmetic Circuit with diagram.
  3. Discuss arithmetic operations performed by Arithmetic Unit.
- 

## 14 Marks

1. Explain Design of Arithmetic Unit with neat block diagram.
  2. Discuss various arithmetic operations performed by Arithmetic Unit.
  3. Explain Arithmetic Unit using Full Adders and Multiplexers.
- 

## PYQ Trend Analysis

| Topic                  | Frequency |
|------------------------|-----------|
| Arithmetic Unit Design | ★★★★★     |

|                             |       |
|-----------------------------|-------|
| Arithmetic Operations Table | ★★★★  |
| Full Adder Based Design     | ★★★★★ |
| Multiplexer Role            | ★★★★  |

---

## Expected 2026 Questions

- 🔥 Explain Design of Arithmetic Unit with block diagram.
  - 🔥 Explain arithmetic operations performed by Arithmetic Unit.
  - 🔥 Discuss role of Full Adder and Multiplexer.
  - 🔥 Explain Arithmetic Unit using selection variables.
- 

## One-Minute Revision

✓ Arithmetic Unit = Part of ALU

✓ Components:

- Full Adder
- Multiplexer
- Registers

✓ Operations:

- Addition
- Subtraction
- Increment
- Decrement
- Transfer

✓ Formula:

$$A - B = A + 2's \text{ Complement}(B)$$

✓ Selection Variables:

$S_1, S_0, C_{in}$

## Conclusion

Arithmetic Unit CPU ka ek important component hai jo binary arithmetic operations perform karta hai. Iska design Full Adders, Multiplexers aur Control Signals par based hota hai. Arithmetic Unit Addition, Subtraction, Increment, Decrement aur Transfer operations ko efficiently execute karta hai aur Computer Architecture me central role nibhata hai. 🎯

### Exam Tip (RGPV 14 Marks)

Answer me ye sequence follow karo:

1. Definition
2. Need of Arithmetic Unit
3. Block Diagram
4. Components
5. Working
6. Arithmetic Operations Table
7. Role of Full Adder
8. Role of Multiplexer
9. Advantages
10. Applications
11. Conclusion

Is format me likhne par answer **3–4 pages** aasani se bhar jayega aur full marks ke chances bahut badh jayenge.